- 1. Find the largest three-digit number which is not a multiple of 3, but is a multiple of the sum of its digits.
- 2. A town has eight neighborhoods named *S*, *T*, *A*, *N*, *F*, *O*, *R*, and *D*. The town mayor plans to rename every neighborhood using each of the letters *G*, *A*, *S*, *H*, *W*, *O*, *R*, and *M* once. In how many ways can the neighborhoods be renamed such that no neighborhood has the same name before and after the renaming?
- 3. The numbers 1, 2, ..., 9 are put in a 3 × 3 grid. Below each column, Alice writes the product of the three numbers in that column, and she adds up her three results to get *A*. Besides each row, Bob writes the product of the three numbers in the row, and adds his three results to get *B*. Given that *A* is as small as possible, what's the maximum possible value of *B*?