

**Time limit:** 15 minutes.

**Instructions:** This tiebreaker contains 3 short answer questions. All answers must be expressed in simplest form unless specified otherwise. You will submit answers to the problem as you solve them, and may solve problems in any order. You will not be informed whether your answer is correct until the end of the tiebreaker. You may submit multiple times for any of the problems, but **only the last submission for a given problem will be graded**. The participant who correctly answers the most problems wins the tiebreaker, with ties broken by the time of the last correct submission.

**No calculators.**

1. George is drawing a Christmas tree; he starts with an isosceles triangle  $AB_0C_0$  with  $AB_0 = AC_0 = 41$  and  $B_0C_0 = 18$ . Then, he draws points  $B_i$  and  $C_i$  on sides  $AB_0$  and  $AC_0$ , respectively, such that  $B_iB_{i+1} = 1$  and  $C_iC_{i+1} = 1$  ( $B_{41} = C_{41} = A$ ). Finally, he uses a green crayon to color in triangles  $B_iC_iC_{i+1}$  for  $i$  from 0 to 40. What is the total area that he colors in?
2. The incircle of  $\triangle ABC$  is centered at  $I$  and is tangent to  $BC$ ,  $CA$ , and  $AB$  at  $D$ ,  $E$ , and  $F$ , respectively. A circle with radius 2 is centered at each of  $D$ ,  $E$ , and  $F$ . Circle  $D$  intersects circle  $I$  at points  $D_1$  and  $D_2$ . The points  $E_1, E_2, F_1$ , and  $F_2$  are defined similarly. If the inradius of  $\triangle ABC$  is 5, what is the ratio of the area of the triangle whose sides are formed by extending  $D_1D_2$ ,  $E_1E_2$ , and  $F_1F_2$  to the area of  $\triangle ABC$ ?
3. Let  $\triangle ABC$  be a triangle with  $BA < AC$ ,  $BC = 10$ , and  $BA = 8$ . Let  $H$  be the orthocenter of  $\triangle ABC$ . Let  $F$  be the point on segment  $AC$  such that  $BF = 8$ . Let  $T$  be the point of intersection of  $FH$  and the extension of line  $BC$ . Suppose that  $BT = 8$ . Find the area of  $\triangle ABC$ .